

1 PipeMaster: inferring population divergence and demographic history with approximate
2 Bayesian computation and supervised machine-learning in R

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9 **Abstract**

10 Understanding population divergence involves testing diversification scenarios and
11 estimating historical parameters, such as divergence time, population size and migration rate.
12 There is, however, an immense space of possible highly parameterized scenarios that are
13 difficult or impossible to solve analytically. To overcome this problem researchers have used
14 alternative simulation-based approaches, such as approximate Bayesian computation (ABC)
15 and supervised machine learning (SML), to approximate posterior probabilities of hypotheses. In
16 this study we demonstrate the utility of our newly developed R-package to simulate summary
17 statistics to perform ABC and SML inferences. We compare the power of both ABC and SML
18 methods and the influence of the number of loci in the accuracy of inferences; and we show
19 three empirical examples: (i) the Muller's termite frog genomic data from Southamerica; (ii) the
20 cottonmouth and (iii) and the copperhead snakes sanger data from Northamerica. We found that
21 SML is more efficient than ABC. It is generally more accurate and needs fewer simulations to

22 perform an inference. We found support for a divergence model without migration, with a recent
23 bottleneck for one of the populations of the southamerican frog. For the cottonmouth we found
24 support for divergence with migration and recent expansion and for the copperhead we found
25 support for a model of divergence with migration and recent bottleneck. Interestingly, by using
26 an SML method it was possible to achieve high accuracy in model selection even when several
27 models were compared in a single inference. We also found a higher accuracy when inferring
28 parameters with SML.

29 **Keywords:** phylogeography, *Dermatonotus*, *Agkistrodon*, UCE, coalescent model

30 **Introduction**

31 The process of population divergence and speciation is finally being realized across
32 many non-model organisms with the use of genetic data and advanced statistical models.
33 Understanding population divergence involves testing diversification scenarios and estimating
34 historical parameters, such as divergence time, historical demography and migration rate
35 (Nielsen & Beaumont, 2009). Under simple diversification scenarios it is possible to use the
36 coalescent model (Kingman, 1982) with the likelihood function and MCMC to infer model
37 probabilities and associated historical parameters (Beerli & Palczewski, 2010; Bouckaert et al.,
38 2014; Gronau, Hubisz, Gulko, Danko, & Siepel, 2011; Hey, 2010; Yang & Rannala, 2010). There
39 is, however, an immense space of possible diversification scenarios where several hypotheses
40 may translate into complex, highly parameterized models that are difficult or impossible to solve
41 analytically (Fagundes et al., 2007; Mayr, 1942).

42 To overcome these limitations, researchers have used alternative approaches to
43 approximate posterior probabilities or marginal likelihoods of population parameters by reducing

44 data to summary statistics (Beichman, Huerta-Sanchez, & Lohmueller, 2018). These summary
45 statistics can be used in approximate Bayesian computation (ABC) and Supervised Machine
46 Learning (SML) to test hypotheses in a flexible likelihood-free context. ABC uses simulations
47 generated from parameter values sampled from prior probabilities to infer posterior probabilities
48 by applying a rejection algorithm that discards all simulations where the distance to the
49 observed data falls above an arbitrary tolerance level (Beaumont, 2011; Csilléry, Blum,
50 Gaggiotti, & François, 2010). Alternatively, simulated summary statistics can be used in SML as
51 training data (Schridder & Kern, 2018). For the simulated data, the link between population
52 parameters and summary statistics is known, so the algorithm can learn this connection and
53 infer model probability and parameter values for observed summary statistics (Burbrink &
54 Gehara, 2018; Sheehan & Song, 2016). To perform ABC and SML, end-users need to create
55 custom scripts to sample parameters from prior distributions and pass them to a simulator. This
56 requires integration of many different packages in various languages and the user's ability to
57 control this workflow sets the limit on the testable diversity of scenarios and hypotheses.

58 ABC and SML algorithms were already implemented in different packages of the R
59 statistical platform (Csilléry, François, & Blum, 2012; Kuhn, 2008). However, there is currently no
60 R-package to generate simulations for simulation-based model inference. To fill that gap we
61 developed a new R-package, called *PipeMaster*, that can be used to build models, add prior
62 distribution to model parameters, and simulate coalescent data from these prior distributions.
63 *PipeMaster* can also calculate summary statistics for the empirical data to allow statistical
64 comparison between observed and simulated data.

65 Here we demonstrate the utility of our newly developed package for three empirical
66 examples and evaluate the power of ABC versus SML and the influence of the number of loci in
67 the accuracy of model inferences. In the first example, we tested 10 hypotheses of divergence

68 for the Muller's termite frog, *Dermatonotus muelleri*, using newly generated data of 2177 loci of
69 ultra-conserved elements (UCE). In the second and third examples, we tested six different
70 hypotheses for two species complexes of North American vipers, the cottonmouth and the
71 copperhead, using pre-existent multi-locus data (Burbrink & Guiher, 2015). We show that
72 *PipeMaster* can be used with other R-packages to perform model and parameter inference in a
73 single platform and to test complex diversification hypotheses to better understand the evolution
74 of organisms.

75 **Material and Methods**

76 The PipeMaster R-package is currently available on github
77 (www.github.com/gehara/PipeMaster) and can be installed via the *install_github* function from
78 the devtools R-package. Below we describe the main features of the package and exemplify its
79 use for model and parameter inference using empirical data with Nexgen and Sanger
80 dimensions.

81 **The interactive menu**

82 *PipeMaster* has an interactive menu that allows the user to build models and set up
83 parameter priors. In addition, the *main.menu* function can take a *ms* simulator string (see
84 Hudson, 2002 for more information about *ms*) for model specification, which can be generated
85 interactively with the PopPlanner application (see Ewing, Reiff, & Jensen, 2015 for more
86 information about this application). Alternatively, the user can input a tree topology in newick
87 format as a backbone of a diversification model, thus generating a simple isolation model with
88 constant population size and divergence time parameters. This basic isolation model can be
89 modified by adding ancestral population size changes and migration parameters, or by removing

90 divergence parameters to simulate island models. The user can use the interactive menu to set
91 conditions for parameter sampling (e.g. $N_{e1} > N_{e2}$: effective population size of population 1 is
92 larger than effective population size of population 2). In the current version, uniform and normal
93 prior distributions are allowed. When the user exits the menu, the model can be saved as an R
94 object. A previously generated model object can be used as a template for a different model
95 setup, eliminating the need to start from the beginning when generating a nested model.
96 Specific characteristics of the data regarding number of base pairs and samples per population
97 per gene can be obtained using the *get.data.structure* function. This function reads the
98 parameters of the observed data and replicates them in the model.

99 **The simulation functions work-flow**

100 *PipeMaster* uses *ms* (Hudson, 2002) as an internal R function, or *msABC* (Pavlidis &
101 Laurent, n.d.) as the essential source of simulation. The program *ms* simulates coalescent trees
102 under the Wright-Fisher model, and places segregating sites on these trees under the infinite
103 site model.

104 *PipeMaster* has three simulation functions for non-hierarchical models: i)
105 *sim.ms.sumstat*, used to simulate summary statistics optimized for Sanger-scale data; ii)
106 *sim.coaltrees*, to simulate coalescent trees; and iii) *sim.msABC.sumstat*, to simulate summary
107 statistics using the simulator *msABC* (Pavlidis, Laurent, & Stephan, 2010) as an external
108 program (**Figure 1a-c**). All functions take as input the model object generated by the *main.menu*
109 function. They have the same basic work-flow and are used to sample parameter values from
110 prior distributions, convert the values to coalescent scale, pass those values to a coalescent
111 simulator, and write the output in a text file. In the case of *sim.ms.sumstat*, the simulated data is
112 passed to PopGenome R-package (Pfeifer, Wittelsburger, Ramos-Onsins, & Lercher, 2014) for

113 summary statistics calculation and the entire simulation process is performed without calling any
114 external program.

115 **ABC and SML analyses**

116 We implemented two different simulation-based inference methods in this study,
117 approximate Bayesian computation (ABC) and supervised machine-learning (SML). In all
118 empirical examples, before proceeding with the inference, we evaluated model-fit by running a
119 PCA of simulated and observed data. For the ABC approach we used the *abc* R-package
120 (Csilléry et al., 2012). We performed an abc rejection using the *postpr* function to calculate
121 model probabilities by retaining 100 simulations with the closest distance from our observed
122 data. To calculate accuracy in model selection we used *cv4postpr* with 100 pseudoreplicates per
123 model and the same tolerance value. The final accuracy was calculated by dividing the total
124 number of correct classifications by the total number of pseudoreplicates.

125 For SML we used the simulated data to train a neural network with one hidden layer to
126 classify the data into different simulated scenarios using the *nnet* algorithm in *caret* R-package.
127 We preprocessed the summary statistics by centering and scaling the data. We used 75% of the
128 simulations as training data and the remaining 25% as testing data. To tune the parameters of
129 the neural network, such as number of nodes and decay value, we performed 10 bootstraps
130 with a maximum of 2,000 iterations in each learning replicate and retained the parameters
131 yielding the highest accuracy. After training and testing, we used the neural network to classify
132 our observed summary stats.

133 To estimate parameters we used the *abc* function of the *abc* R-package with the
134 *neuralnet* regression method. Before proceeding with the estimation we simulated additional
135 data for the best selected model totalizing 1,000,000 data sets for the Sanger examples and

136 100,000 for the UCE example. The *abc* function first performs a rejection step, reducing the
137 dataset before neural network training. We evaluated tolerance and the accuracy of parameter
138 estimates using the *cv4abc* function with 100 replicates and two different tolerance values for
139 the Sanger examples (0.01, 0.001) and three values for the UCE example(0.1, 0.01, 0.001) . We
140 then calculated the correlation (r) between true and estimated parameters for each tolerance
141 value. We selected the tolerance yielding the best correlations among parameters. All codes
142 used in the ABC and SML are available on github as part of a tutorial for the package
143 (github.com/gehara/PipeMaster).

144 **SML versus ABC and the influence of the number of loci in the accuracy of estimates**

145 To evaluate the influence of the number of loci and compare the performance of ABC
146 versus SML for estimating the true model, we ran a set of simulations experiments with four
147 treatments that varied in total number of loci (10, 100, 1000, 2177). We used the case study of
148 *Dermatonotus muelleri* below as an empirical basis for this experiment. Accordingly, simulation
149 parameters, models, priors and summary statistics were the same as simulated for *D. muelleri*,
150 while the different number of loci with their parameters (base pairs number of individuals per
151 population) were obtained by sub-sampling 10, 100, or 1000 loci from the total dataset of 2177
152 loci generated for *D. muelleri*, plus a fourth treatment that contained the entire dataset. In each
153 treatment we ran ABC and SML inferences for a group of pseudo-observed data (POD; i.e. test
154 data in machine-learning jargon). We repeated these calculations three times, varying the total
155 number of simulations per model (1,000, 10,000 and 100,000).

156 We also performed a simulation experiment based on the *D. muelleri* data to evaluate
157 the accuracy of parameter estimates under different number of loci. In this case we estimated
158 parameters for 100 POD under the IsBott2 model, which was the model with the highest

159 probability for *D. muelleri* (see details below). We simulated a total of 100,000 data sets to use
160 as reference data. To estimate parameters we used the *abc* function of the *abc* R-package with
161 the neural network regression. We retained 1000 simulations after the rejection step and used
162 these to train a neural network. We then calculated the correlation (r) between true value and
163 estimated value for each parameter. An r closer to 1 would indicate a lower error in parameter
164 estimates. We performed this calculation for the same treatments of 10, 100, 1000 and 2177 loci
165 and we tested different retention or tolerance values.

166 **Application with UCE data - testing diversification hypotheses for muller's termite frog**

167 As an empirical example we generated a dataset of 2177 loci of ultra-conserved
168 elements (UCE) for the neotropical frog, *Dermatonotus muelleri* (see details of molecular
169 protocol in the Supplementary methods). This species is distributed along the dry diagonal of
170 open formations which separates the Amazon from the Atlantic Forest. It is an explosive
171 breeder, highly adapted to seasonal environments with pronounced periods of drought (Nomura,
172 Rossa-Feres, & Langeani, 2009). A previous study using three loci (Oliveira et al., 2018) found
173 that *D. muelleri* is composed by two deeply divergent populations, one distributed in the
174 Caatinga and north of Cerrado, and a second one distributed in the southwest part of Cerrado
175 (**Figure 2a**). Here we took a subsample of 88 individuals used in that study. After data assembly
176 population assignment tests (see Supplementary methods) confirmed the existence of two
177 spatially structured clusters (Oliveira et al., 2018).

178 The geographic break separating these two populations falls in an area of high elevation,
179 which may have isolated the populations. Also, Pleistocene climatic cycles are expected to have
180 influenced the demographic history of at least the Northeast population (Gehara et al., 2017;
181 Oliveira et al., 2018). Oliveira et al. (2018) found support for a model of diversification without

182 migration and expansion only for the Northeastern population. To challenge these findings and
183 test alternative diversification hypotheses for *D. muelleri*, we tested 10 two-population models:
184 (i) a pure isolation scenario without migration and without demographic change (Is); (ii) an
185 isolation with migration scenario without demographic change (IM); (iii) an isolation with recent
186 expansion and no migration (IsExp); (iv) an isolation with migration and recent expansion
187 (IMExp); (v) isolation with recent bottleneck and expansion (IsBott); (vi) isolation with migration,
188 recent bottleneck and expansion (IMBott); (vii) isolation with recent expansion only for the
189 Northeastern population (IsExp2); (viii) isolation with migration with expansion only for the
190 Northeastern population (IMExp2); (ix) an isolation with bottleneck only for the Northeastern
191 population (IsBott2); (x) an isolation with migration scenario with a bottleneck only for the
192 Northeastern population (IMBott2) (**Figure 3**). Priors of population sizes and time of
193 demographic events were retrieved from Oliveira et al. (2018) and can be found in the
194 **Supplementary Table 1**.

195 We simulated 100,000 data sets of 38 summary statistics (see **Supplementary**
196 **Methods** and tutorial: github.com/gehara/PipeMaster) per model with *sim.msABC.sumstat*
197 function. We used two independent approaches for model inference, ABC and SML described
198 above.

199 **Application with Sanger data - testing diversification hypotheses for Copperhead and** 200 **Cottonmouth pit vipers**

201 We also performed a model selection for two species complexes of vipers widely
202 distributed in Eastern North America: the *Agkistrodon contortrix* complex (Copperheads), and
203 the *Agkistrodon piscivorus* complex (Cottonmouths). The dataset used contain one
204 mitochondrial and five nuclear loci.

205 The *A. contortrix* species complex comprises two species, *A. contortrix* and *A.*
206 *laticinctus*, which together cover a large portion of eastern and central United States.
207 *Agkistrodon contortrix* is associated with deciduous hardwoods and pine forests and has a wider
208 distribution in the Eastern and Midwestern US (**Figure 2b**). *Agkistrodon laticinctus* occurs in
209 drier grassland environments in the central US to the Trans-Pecos habitats of west Texas.
210 Diversification in this complex is likely ecological, since their contact zone falls in the transition
211 from forested habitats to grasslands (Burbrink & Guiher, 2015). Both species currently occur in
212 areas that were covered by ice sheet during the last glaciation and show genetic signs of
213 population expansion in the Pleistocene (Guiher & Burbrink, 2008).

214 The *A. piscivorus* is also composed of two species. One of them, *A. conanti*, is mainly
215 restricted to the Florida Peninsula. The other, *A. piscivorus*, is distributed north of the peninsula
216 up to southern Illinois and Indiana in the north, Eastern Texas in the west, and coastal North
217 Carolina in the east (**Figure 2c**). The contact zone of these two species in the Florida peninsula
218 represents a common phylogeographic break for several other organisms (Burbrink, Fontanella,
219 Alexander Pyron, Guiher, & Jimenez, 2008; Krysko, Nuñez, Lippi, Smith, & Granatosky, 2016;
220 Mckelvy & Burbrink, 2017; Soltis, Morris, McLachlan, Manos, & Soltis, 2006) and the
221 diversification of the complex was also likely influenced by the climatic cycles of the Quaternary
222 (Guiher & Burbrink, 2008).

223 Taking these aspects into account, we tested for both species complexes, six
224 diversification hypotheses (**Figure 3**). We generated the six models (a subset of the models
225 simulated for the frog example above; see **Figure 3**) and simulated 100,000 datasets for each
226 model using the *sim.ms.sumstat* function of PipeMaster R-package. We used wide uniform prior
227 distributions according to Burbrink and Guiher (2015) (see parameter list and priors in the

228 supplementary material). We used a set of 17 summary statistics (see **Supplementary**
229 **Methods** and tutorial: github.com/gehara/PipeMaster)

230 For both species complexes and both methods used (ABC and SML) we compared the
231 models hierarchically. (i) first we compared all the Isolation models with each corresponding
232 version that included migration (e.g. IsD against IMD; IsBott against IMBott). (ii) Then we took
233 the best models resulting from the first comparisons and conducted a second comparison to find
234 the best model of all.

235 **Results**

236 **SML versus ABC**

237 The simulation experiment shows a higher error in model selection when using ABC
238 relative to SML (**Figures 4 and 5**). The number of loci has a strong influence in the accuracy of
239 model inferences. The dataset with 2177 loci had highest accuracy while the 10 locus dataset
240 had the lowest. The number of simulations also influence accuracy with inferences performed
241 with a reference dataset of 1,000 simulations per model having the lower true model
242 probabilities (**Figure 4**), while the inferences performed with 100,000 simulations per model has
243 the highest, particularly for ABC. For the SML inference both reference datasets of 10,000 and
244 100,000 simulations per model yielded nearly identical accuracies. The number of loci also has
245 influence in parameter estimates. SML had higher precision when compared to ABC (**Figure 5**).
246 The number of retained simulations, the tolerance value, influences ABC and SML in different
247 ways. For ABC retaining a low number of simulations yielded higher R . For SML retaining more
248 simulations result in better algorithm training.

249 **Diversification of muller's termite frog**

250 Simulations presented a good fit to the data as shown by the PCA plots
251 (**Supplementary Figure 1**). The trained neural network is able to differentiate and classify the
252 10 models with an accuracy of 0.879 while the ABC had an accuracy of 0.83. Using the SML
253 approach the observed data was classified as the IsBott2 model with a probability higher than
254 0.99 (**Table 1**), where only the northeast population experienced a bottleneck with expansion.
255 The ABC inference suggest a different model, IMexp, where the two populations expand after
256 divergence. In this case, the probability of the model was considerably lower, 0.49. Because the
257 accuracy of the SML is higher, we consider the IsBott2 as the best model.

258 The divergence time can be estimated with high accuracy and suggest a split around 2.6
259 Ma between the two populations (**Table 2**). Estimated current sizes for population 1 suggest a
260 very large population after expansion but accuracy of this estimate is low. Estimates for
261 population 2 are more accurate (**Table 2**). The average estimated mutation rate was
262 $2.2E-10$ /site/generation with an estimated standard deviation of $3.88E-10$ /site/generation.

263 **Diversification of Copperhead and Cottonmouth pit vipers**

264 For both species complexes, the simulated models had a good fit to the data, as
265 suggested by the PCA (**Supplementary Figure 2**). In the first comparisons (1, 2 and 3; see
266 **Table 3**) for the *A. contortrix* complex, the accuracy varied from 0.79 – 0.85 for the SML and
267 from 0.76 – 0.86 for the ABC. For comparison 1 (Is vs IM), ABC and SML showed conflicting
268 results, with the pure isolation model, Is, having the highest probability for the ABC and the
269 isolation with migration model, IM, having the highest probability in the SML. For comparisons 2
270 and 3, the two methods showed concordant results; models that included migration had higher
271 probabilities than the correspondent models without migration (**Table 3**). The final comparison
272 accuracies of ABC and SML were 0.78 and 0.79 respectively. Both methods converged in the
273 same best model for the diversification of *A. contortrix* complex, IMBott (**Table 3**). For all

274 comparisons, the SML showed higher probabilities for the selected model when compared to
275 ABC (**Table 3**).

276 In the first comparisons (1, 2 and 3; see **Table 3**) for the *A. piscivorus* complex, the
277 accuracy varied from 0.92 – 0.94 for the SML and from 0.89 – 0.93 for the ABC, and the best
278 selected model were the same as the ones inferred for the *A. contortrix* complex (**Table 3**). In
279 the final comparison, the accuracy of the ABC was higher than the SML, 0.87 and 0.79
280 respectively. However, both methods suggest high probabilities for the same model, the IMexp,
281 which is an isolation with migration with expansion for both species (**Table 3**).

282 The cross-validation for the parameter estimates suggest low correlation between
283 estimated and true values, particularly for *A. contortrix* (**Table 4**), suggesting high uncertainty in
284 estimates. In general, the parameters that can be estimated with higher confidence are the
285 current population sizes (**Table 4**).

286 **Discussion**

287 Our simulation experiment showed that supervised machine-learning outperforms
288 approximate Bayesian computation. This is particularly evident for datasets with genomic
289 dimensions, which is the current standard of molecular studies for non-model organisms. We
290 also show that much higher accuracies can be obtained with a SML as opposed to ABC, even
291 when using just 100 loci and a considerably low number of simulations per model (10,000).
292 Thus, because ABC requires a larger amount of simulations, it is more time consuming and less
293 efficient when compared to SML.

294 Our simulation experiment also show that the model parameters can be estimated with
295 higher accuracy with the increase in the number of loci. The SML approach also outperforms
296 ABC for parameter estimates (**Figure 4**). Some parameters, like current effective population

297 size and time of divergence, can be estimated with higher accuracy. However, ancestral
298 population sizes are harder to estimate (**Figure 5; Table 2**). Interestingly, posterior distributions
299 of the average and standard deviation of the mutation rate across all loci can be obtained with
300 high confidence, allowing a more relaxed assumption when compared to using a fixed mutation
301 rate for all loci.

302 **Diversification of muller's termite frog**

303 We found support for an isolation model with population contraction with expansion for
304 the northeast population. This partially agrees with Oliveira et al. (2018), who found support for
305 recent expansion without a contraction. Oliveira et al. (2018) analyzed only three loci while we
306 analyzed more than 2,000, thus our data certainly contains more information about historical
307 demography (e.g. Gill et al., 2013).

308 The inference of a population contraction in the northeast population reinforces the idea
309 of dynamic landscape changes in the northeast of Brazil along the Pleistocene. Currently, this
310 area is predominantly covered by the Caatinga semiarid environment, but many studies suggest
311 periods of increase in humidity in the last 1 Ma (Auler et al., 2004b; Cheng et al., 2013).
312 Travertine deposits suggest a long period of increase in humidity from approximately 460 to 330
313 K years (Auler et al., 2004a) which remarkably agrees with our estimated time for the reduction
314 in population size (mode: 337 Ky, CI: 195 – 437 Ky). These humid phases in the northeast of
315 Brazil may have allowed long distance dispersals between Amazon and Atlantic forest fauna
316 (Dal Vechio, Prates, Graziotin, Zaher, & Rodrigues, 2018; Prates, Rivera, Rodrigues, &
317 Carnaval, 2016). The reduction in population size is followed by a population expansion starting
318 at around 230 K years (CI: 132 – 362 K years), in agreement of other studies that find
319 synchronous population expansion Caatinga's herpetofauna (Gehara et al., 2017).

320 The estimated divergence time at 2.6 Ma is considerably younger than previous
321 estimates (~4 Ma; see Oliveira et al., 2018). Our estimates places the divergence between the
322 northeast and southwest populations in the Pliocene-Pleistocene transition, after the mid
323 Pliocene warm period, when the average global temperature was 2 – 3° C higher than today.
324 This higher temperature may have allowed *D. muelleri*, a lowland species, to inhabit the
325 highlands of the Brazilian plateau. With the temperature cooling the highland climate may have
326 become unsuitable for the species and the Brazilian plateau became a vicariant barrier causing
327 diversification.

328 **Diversification of Copperhead and Cottonmouth pit vipers**

329 For both species complexes, we found support for demographic change and gene flow
330 between species pairs. For the *A. contortrix* complex, we found support for a reduction in
331 population size with subsequent expansion in the late Pleistocene. This species complex is
332 currently found in areas that were covered by ice sheets during glaciations. Accordingly, the
333 glacial cycles would have restricted the distribution of the species to southern refugia,
334 causing a population contraction (Burbrink et al., 2016; Marshall, James, & Clarke, 2002). In
335 interglacial periods, the species would expand their range and their population sizes. It is also
336 possible that the climatic cycles influenced their divergence, driving speciation by the isolation of
337 populations in distinct refugia. Nevertheless, the presence of gene flow indicates that if isolation
338 happened during glaciations, they were likely followed by periods of contact. Gene flow may
339 also indicate the role of climatic gradients in diversification. *Agkistrodon contortrix* and *A.*
340 *latiscinctus* occur in distinctly different niches (Burbrink & Guiher, 2015; Gloyd & Conant, 1990)
341 and they likely present physiological adaptations to these different environments. Thus, hybrids
342 may have lower fitness when compared to non-hybrids (Gow, Peichel, & Taylor, 2007). Future

343 studies using thousands of loci will have the opportunity to test for selection across the climatic
344 gradients, and may shed more light on the evolution of the *A. contortrix* species complex.

345 For the *A. piscivorus* complex, we found no support for a bottleneck during the
346 Pleistocene. The most probable model suggests an isolation with gene flow and a recent
347 population expansion. Both *A. piscivorus* and *A. conanti* are mostly distributed in areas free from
348 broadscale effects of Pleistocene glaciation (Marshall et al., 2002). Accordingly, the supported
349 model suggests a relatively more stable population size, with recent population expansion for
350 both species. The contact zone between the species is in the northern area of the Florida
351 Peninsula. This region was isolated from the continent when sea levels were higher, so it is
352 likely that the diversification of the complex was influenced by sea level rise, which could have
353 isolated *A. conanti* in a continental island formed by part of the landmass that today represents
354 the Florida Peninsula (Hine, 2013; Krysko et al., 2016). In this scenario, gene flow between *A.*
355 *conanti* and *A. piscivorus* was favored during glacial periods when sea levels were low, while
356 isolation happened during interglacial periods while sea levels were high.

357 **Conclusion**

358 We demonstrated the use of coalescent simulations generated by our newly developed
359 R-package to infer the probability of complex diversification models in three different non-model
360 organisms. In the three cases, we were able to test relatively complex demographic models with
361 population size change, population structure and migration that are difficult, time consuming or
362 impossible to implement using a full Bayesian or likelihood approaches. Interestingly, by using a
363 SML method it was possible to achieve high accuracy in model selection even when several
364 models were compared in a single inference (**Table 1**).

365 Machine-learning algorithms are becoming increasingly available to the general scientific
366 community through R and Python applications, facilitating its use for an unprecedented number
367 of cases in evolutionary biology and ecology. Here we demonstrated its use comparing it with a
368 more traditional, ABC, for model inference in population genetics. Our results agree with the
369 recent literature (Schrider & Kern, 2018; Sheehan & Song, 2016) supporting the power of SML
370 in dealing with complex multi-dimensional problems such as the ones presented here.

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373 gathering the data; and Brian T. Smith, Gustavo Cabanne and Gregory Thom e Silva for trying
374 beta versions of the package.

375 **Author Contributions**

376 MG and FB conceived the ideas; MG, GGM and FB designed methodology; FB and MG
377 collected the data; MG analyzed the data; MG and FB led the writing of the manuscript. All
378 authors contributed critically to the drafts and gave final approval for publication.

379 **Data Availability**

380 All codes used in the ABC and SML analyses are found in
381 github.com/gehara/PipeMaster. The assembled UCE data is available in the Dryad (upon
382 manuscript acceptance).

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500 **Tables**

501 **Table 1:** Model probabilities and accuracies calculated with ABC and SML for the comparison of
 502 10 simulated models for the frog *Dermatonotus muelleri* 2177 UCE data. (see **Figure 3** for a
 503 schematic representation of the models).

Model	Probability	
	SML	ABC
IM	0	0
IMBott	0	0.17
IMBott2	0	0
IMExp	0	0.49
IMExp2	0	0
Is	0	0
IsBott	0.0037	0.17
IsBott2	0.9963	0.13
IsExp	0	0
IsExp2	0	0.04
Accuracy	0.8798	0.826

504 **Table 2:** Parameter priors, posterior estimates and correlation (*r*) result calculated with the
 505 cross-validation experiment for the frog species (UCE data). See **Supplementary Table 1** for a
 506 complete list of priors and parameters.

Paramater	Prior (min – max)	2.50%	Median	Mean	Mode	97.50%	<i>r</i>
Ne0.pop1	100,000 – 5,000,000	2,450,945	3,756,958	3,845,324	3,543,630	5,538,957	0.58
Ne0.pop2	100,000 – 5,000,000	-347,089	1,012,398	1,007,289	993,517	2,270,467	0.82
Ne1.pop1	1,000 – 50,000	5,275	24,930	24,360	31,128	39,783	0.55
Ne2.pop1	50,000 – 5,000,000	1,784,442	3,633,865	3,728,091	3,342,328	5,908,761	0.2
Ne1.pop2	50,000 – 5,000,000	-727,952	123,083	133,108	132,045	1,166,070	0.82
join1	500,000 – 8,000,000	1,139,788	2,615,899	2,600,426	2,620,037	4,173,138	0.84
t.Ne1.pop1	20,000 – 500,000	132,078	238,909	241,542	233,411	362,085	0.64
t.Ne2.pop1	20,000 – 500,000	195,084	324,834	321,999	336,868	427,928	0.51
t.Ne1.pop2	500,000 – 8,000,000	1,002,084	2,470,257	2,453,955	2,464,068	3,996,727	0.84
mean.rate	1E-11 – 1E-9	6.50E-11	2.28E-10	2.38E-10	2.27E-10	5.04E-10	0.77
sd.rate	1E-11 – 1E-9	2.71E-10	3.99E-10	4.12E-10	3.88E-10	6.50E-10	0.79

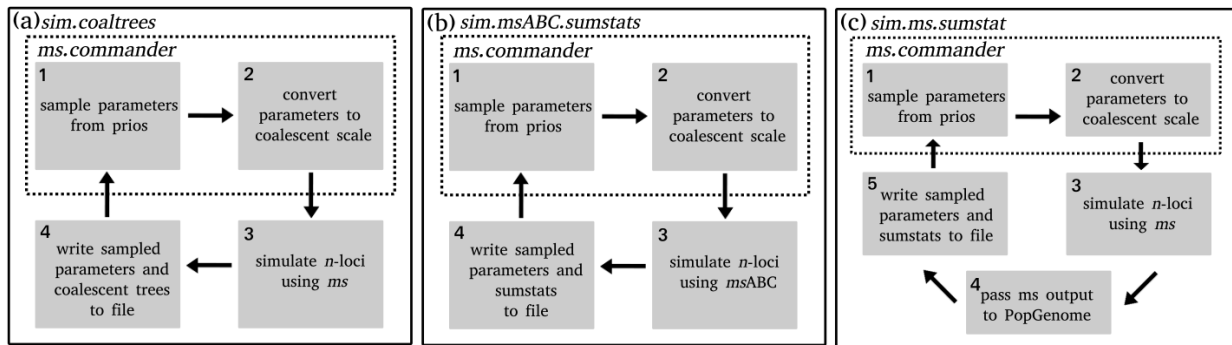
507 **Table 3:** Model probabilities estimated with ABC and SML with respective accuracies of estimates for
 508 the two snake species complex. Models were compared hierarchically, first comparisons 1, 2 and 3 were
 509 carried out independently. The final comparison included the best models of comparison 1, 2 and 3. Bold
 510 probabilities indicate the selected model for each comparison (see Figure 3 for a schematic
 511 representation of the models).

<i>Agkistrodon piscivorus</i>				
	1	2	3	Final
	Is vs IM (Accuracy)	IsExp vs IMExp (Accuracy)	IsBott vs IMBott (Accuracy)	Best 1 vs Best 2 vs Best 3 (Accuracy)
SML	0.11 / 0.89 (0.94)	0.01 / 0.99 (0.94)	0.04 / 0.96 (0.92)	0.01 / 0.85 / 0.14 (0.79)
ABC	0.78 / 0.23 (0.93)	0.19 / 0.82 (0.91)	0.49 / 0.51 (0.89)	0.13 / 0.61 / 0.26 (0.87)
<i>Agkistrodon contortrix</i>				
	1	2	3	Final
	Is vs IM (Accuracy)	IsExp vs IMExp (Accuracy)	IsBott vs IMBott (Accuracy)	Best 1 vs Best 2 vs Best 3 (Accuracy)
SML	0.03 / 0.97 (0.79)	0.00 / 1.00 (0.85)	0.00 / 1.00 (0.79)	0.12 / 0.01 / 0.87 (0.79)
ABC	0.59 / 0.42 (0.76)	0.08 / 0.92 (0.86)	0.18 / 0.82 (0.77)	0.33 / 0.01 / 0.66 (0.78)

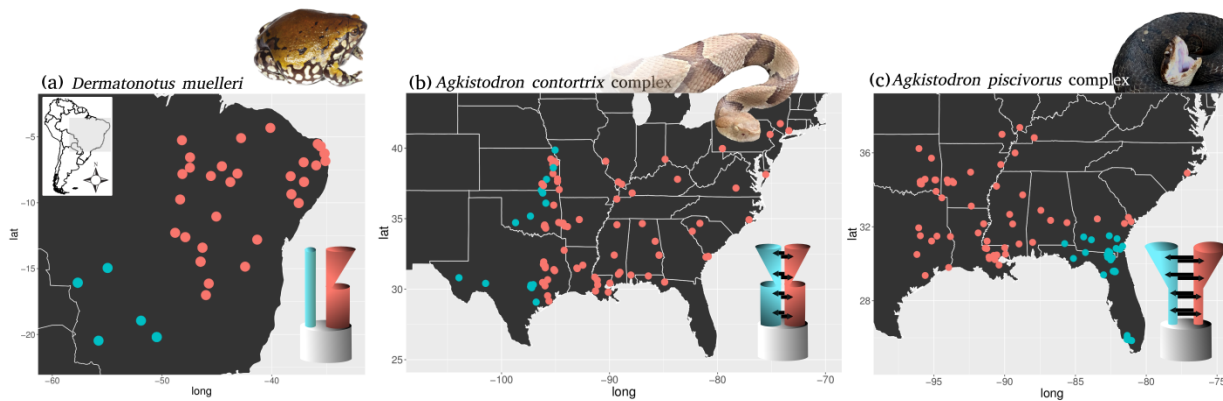
512 **Table 4:** Parameter priors, posterior estimates and R result calculated with the cross-validation
 513 experiment for the two snake species complexes (Sanger data). See **Supplementary Table 1**
 514 for a complete list of priors and parameters.

<i>Agkistrodon contortrix</i>							
Parameter	Prior (min – max)	2.50%	Median	Mean	Mode	97.50%	r
Ne0.pop1	20,000 – 1,000,000	26,112	123,258	140,965	77,843	325,493	0.45
Ne0.pop2	20,000 – 1,000,000	92,136	491,649	506,789	202,242	988,100	0.19
Ne1.pop1	1,000 – 10,000	1,360	7,030	6,637	8,902	9,924	0.06
Ne2.pop1	20,000 – 1,000,000	5,895	556,886	535,324	883,327	967,817	0.01
Ne1.pop2	1,000 – 10,000	1,809	6,932	6,612	9,094	9,910	0.12
Ne2.pop2	20,000 – 1,000,000	303,312	710,668	691,052	850,608	983,683	0.34
join1	60,000 – 3,000,000	285,633	1,625,645	1,611,305	2,039,677	2,874,342	0.06
t.Ne1.pop1	9,000 – 300,000	31,942	127,478	139,292	99,724	289,616	0.46
t.Ne2.pop1	9,000 – 300,000	73,265	191,863	198,353	148,644	346,239	0.38

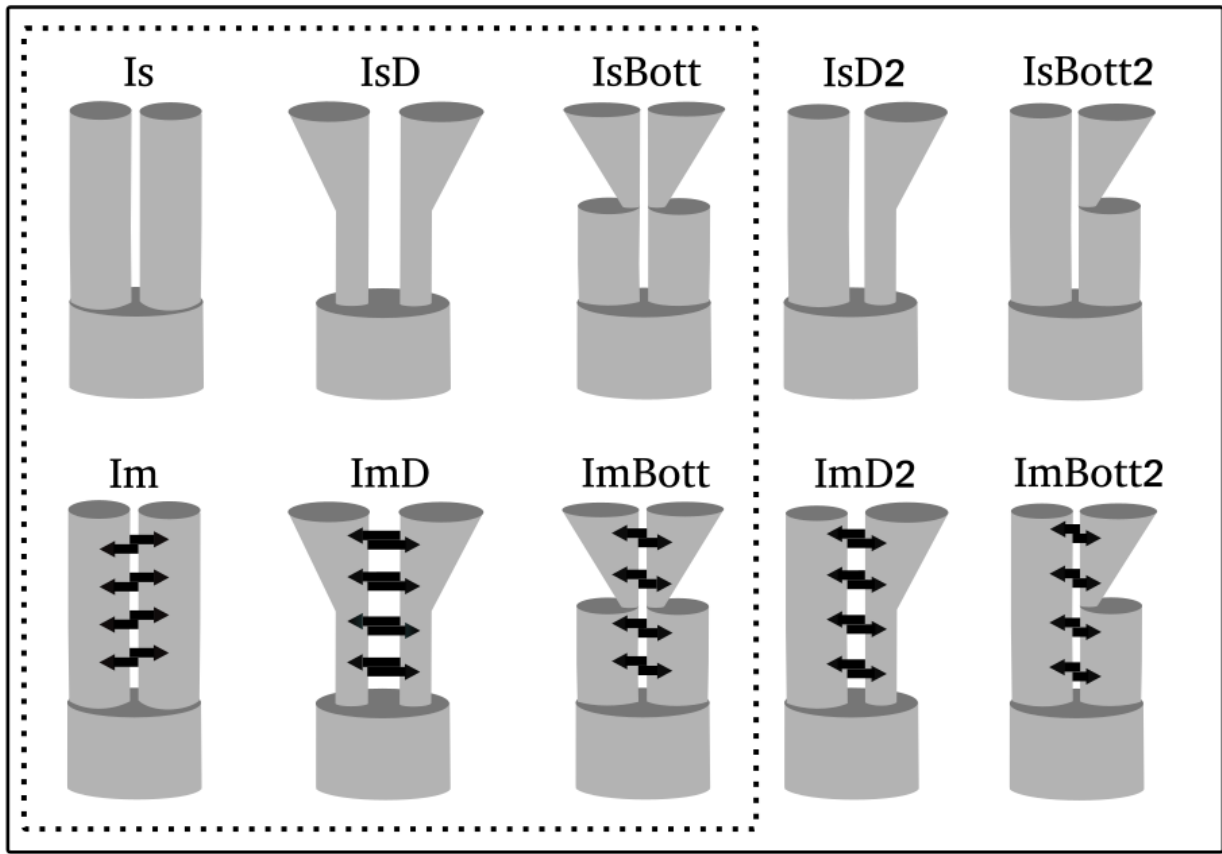
t.Ne1.pop2	9,000 – 300,000	36,938	132,674	140,750	106,220	271,105	0.28
t.Ne2.pop2	9,000 – 300,000	74,227	198,593	197,694	202,263	316,021	0.06
mig0.1_2	0 – 2	0.76	1.5	1.47	1.75	2.06	0.18
mig0.2_1	0 – 2	0.07	1.05	1.04	1.75	1.95	0.06
<i>Agkistrodon piscivorus</i>							
Paramater	Prior (min – max)	2.50%	Median	Mean	Mode	97.50%	r
Ne0.pop1	10,000 – 500,000	104,779	258,656	269,769	198,668	475,458	0.4
Ne0.pop2	10,000 – 500,000	59,975	216,254	236,734	130,139	475,953	0.47
Ne1.pop1	1,000 – 10,000	3,534	41,156	42,827	32,328	89,432	0.42
Ne1.pop2	1,000 – 10,000	8,510	50,965	50,489	54,790	91,127	0.49
Ne2.pop2	10,000 – 1,000,000	163,818	552,602	556,057	564,831	956,823	0.05
join1	9,9000 – 9,900,000	276,722	4,627,486	4,741,277	1,325,740	9,626,987	0.55
t.Ne1.pop1	9,000 – 210,000	20,944	104,030	109,209	53,650	210,963	0.35
t.Ne1.pop2	9,000 – 210,000	-414	79,993	86,828	27,249	195,189	0.53
t.Ne2.pop2	9,900 – 9,900,000	246,730	4,629,289	4,743,890	1,309,786	9,653,230	0.56
mig0.1_2	0 – 2	0.19	0.87	0.93	0.72	1.91	0.28
mig0.2_1	0 – 2	0.03	0.74	0.8	0.51	1.75	0.29



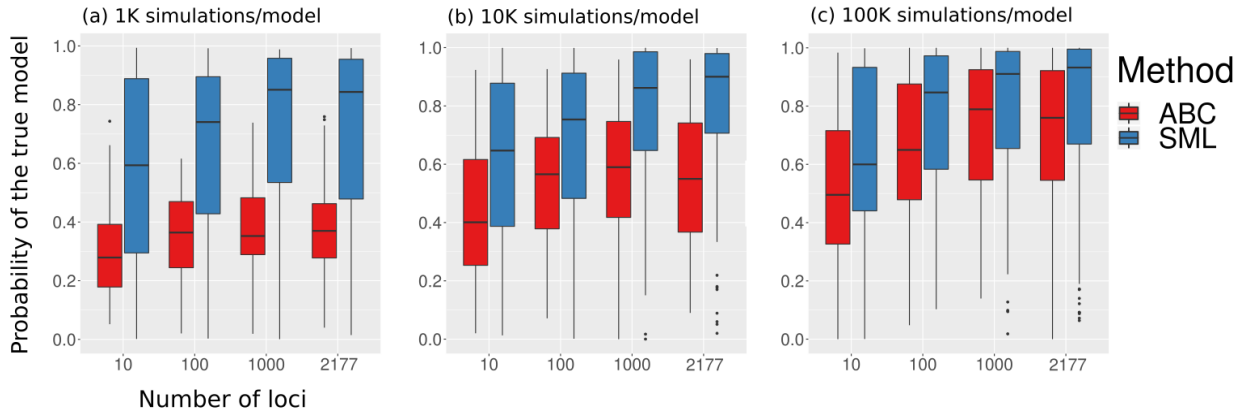
516 **Figure 1:** work-flow of the main simulation functions of PipeMaster and schematic
 517 representation of the simulated models in the toy example. (a) work-flow of the *sim.ms.sumstat*
 518 function; (b) schematic representation of the diversification models simulated in the toy example;
 519 (c) work-flow of the *sim.coaltrees* function; (d) work-flow of the *sim.msABC.sumstat* function.



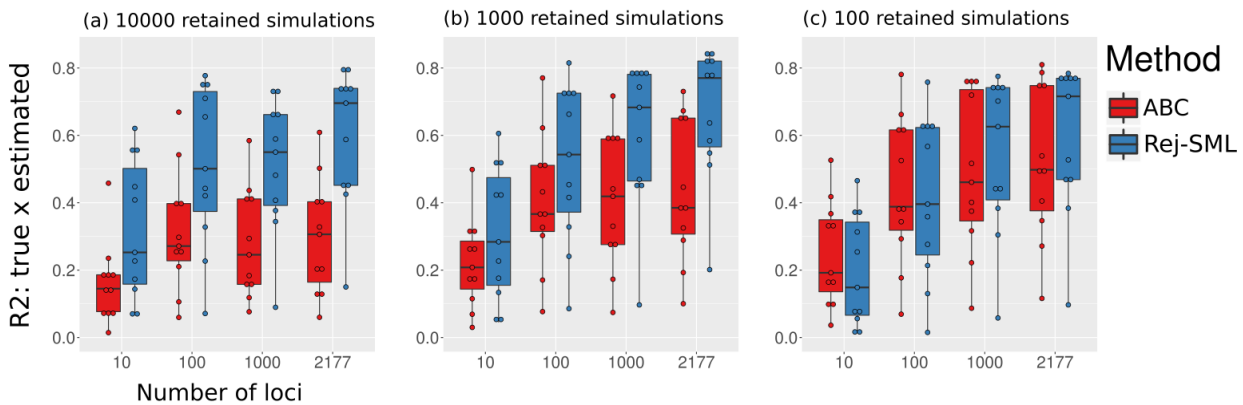
520 **Figure 2:** Distribution maps and best model for each data set analyzed in this study.



521 **Figure 3:** Schematic representation of the diversification models tested in the two *Agkistrodon*
 522 species complexes and *Dermatonotus muelleri*. Dotted line indicate the six models tested for *A.*
 523 *contortrix* and *A. piscivorus* complex. For *D. muelleri* we tested all 10 models. See
 524 **Supplementary Table 1** for a complete list of priors and parameters.



525 **Figure 4:** Results of the simulation experiment to compare the accuracy of ABC and SML for
 526 model inference in different conditions. The y-axis represents the probability of the true model,
 527 the x-axis represent different data dimensions. Each box plot represent probabilities of the true
 528 model for 100 pseudo observed data, 10 per model. For the ABC analysis, 100 simulations are
 529 retained in the rejection step, for the SML all simulations are used for algorithm training. (a)
 530 estimates performed with 1K simulations per model totalizing 10,000 simulations in the
 531 reference table. (b) estimates performed with 10K simulations per model totalizing 100,000
 532 simulations in the reference table. (c) estimates performed with 100K simulations per model
 533 totalizing 1,000,000 simulations in the reference table.



534 **Figure 5:** Results of the simulation experiment to evaluate the influence of number of loci and
 535 tolerance values on parameter estimates of ABC and rejection with SML. The y-axis represents
 536 the correlation between estimated and true values for 100 pseudo-observed data for the 11
 537 parameters of the model. (a) estimates are performed by retaining 10,000 closest simulations.
 538 (b) estimates are performed by retaining 1,000 closest simulations. (c) estimates are performed
 539 by retaining 100 closest simulations.